

Reciprocals

Reciprocals are two fractions that have a product of 1.

Fractions:

To find the reciprocal of a fraction, switch the numerator and denominator.

The reciprocal of $\frac{3}{8}$ is $\frac{8}{3}$.

$$\frac{3}{8} \times \frac{8}{3} = \frac{24}{24} = 1$$

Whole Numbers:

To find the reciprocal of a whole number, first write it as a fraction. Then switch the numerator and denominator.

$$7 = \frac{7}{1}$$

The reciprocal of $\frac{7}{1}$ is $\frac{1}{7}$.

Mixed Numbers:

To find the reciprocal of a mixed number, first write it as a fraction. Then switch the numerator and denominator.

$$5\frac{2}{3} = \frac{17}{3}$$

The reciprocal of $\frac{17}{3}$ is $\frac{3}{17}$.

Are the two numbers reciprocals? Write *yes* or *no*.

1. $\frac{1}{9}$ and 19

2. $\frac{3}{10}$ and $\frac{10}{3}$

3. $1\frac{3}{5}$ and $\frac{8}{5}$

4. 5 and $\frac{1}{5}$

5. $\frac{5}{13}$ and $2\frac{3}{5}$

6. $\frac{1}{10}$ and $\frac{1}{10}$

7. $2\frac{1}{4}$ and $\frac{4}{9}$

8. $\frac{7}{12}$ and $\frac{12}{7}$

Write the reciprocal of each number.

9. $\frac{1}{7}$

10. $\frac{5}{12}$

11. 6

12. $3\frac{5}{9}$

13. $\frac{6}{5}$

14. $\frac{2}{11}$

15. 11

16. $1\frac{3}{8}$

17. $\frac{1}{2}$

18. 100

Divide Whole Numbers by Fractions

Beth is working on a science project. She needs pieces of wire that are $\frac{2}{3}$ yd long for the project. She bought a piece of wire that is 6 yd long at the hardware store.

How many $\frac{2}{3}$ -yd pieces can she cut from this 6-yd piece?

Step 1: Write a division sentence to find this amount.

$$\frac{6}{1} \div \frac{2}{3}$$

Think: Write 6 as $\frac{6}{1}$.

Step 2: Use the reciprocal of the divisor to write a multiplication problem.

$$\frac{6}{1} \times \frac{3}{2}$$

Think: The reciprocal of $\frac{2}{3}$ is $\frac{3}{2}$.

Step 3: Multiply.

$$\frac{6}{1} \times \frac{3}{2} = \frac{18}{2} = 9$$

So, Beth can cut 9 pieces of wire.

Use the reciprocal to write a multiplication problem. Solve the problem. Write the answer in simplest form.

1. $3 \div \frac{1}{8}$

2. $5 \div \frac{1}{2}$

3. $10 \div \frac{2}{3}$

4. $27 \div \frac{3}{5}$

$\frac{3}{1} \times \frac{8}{1} = 24$

5. $12 \div \frac{4}{5}$

6. $8 \div \frac{3}{4}$

7. $18 \div \frac{3}{8}$

8. $7 \div \frac{4}{5}$

9. $6 \div \frac{3}{4}$

10. $16 \div \frac{4}{5}$

11. $9 \div \frac{6}{7}$

12. $2 \div \frac{3}{10}$

13. $9 \div \frac{3}{8}$

14. $9 \div \frac{1}{5}$

15. $6 \div \frac{3}{20}$

16. $20 \div \frac{4}{5}$
